

THE IMPLEMENTATION OF CHAT BOT AI TO ENHANCE METACOGNITIVE INTERACTION IN INTEGRAL CALCULUS: A CASE STUDY ON THE METHOD OF INTEGRATION

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ABSTRACT

This study investigates the integration of Artificial Intelligence (AI) technologies, with a particular emphasis on AI-based chatbots, to enhance metacognitive interactions in the learning of integral calculus, specifically within the domain of integration methods. By cultivating learners' capacities for planning, monitoring, and evaluating their problem-solving strategies, AI-driven interventions act as catalysts for the development of metacognitive awareness in advanced mathematics instruction. Metacognition, which entails both the awareness and regulation of one's cognitive processes, constitutes a critical determinant of effective problem-solving proficiency. Employing a case study design, this research explores the utilization of interactive AI chat prompts to deliver real-time guidance, thereby encouraging students to engage in reflective evaluation of their strategies and cognitive approaches. The efficacy of the AI platform is assessed through targeted interventions aimed at fostering metacognitive engagement and enhancing learning outcomes. The findings demonstrate that AI integration significantly supports students in identifying their cognitive strengths and limitations, while promoting the deployment of effective, adaptive problem-solving strategies. By reinforcing metacognitive interaction, this approach equips learners with the cognitive flexibility necessary to navigate complex mathematical tasks, simultaneously contributing to the progression of innovative, technology-enhanced pedagogical practices. Furthermore, the study highlights the role of AI-facilitated personalized learning and adaptive learning environments in supporting differentiated instruction tailored to individual learner profiles.

Keywords: artificial intelligence in education, metacognitive interaction, adaptive learning technologies, integral calculus instruction, problem-solving strategies

INTRODUCTION

The incorporation of Artificial Intelligence (AI) in education has garnered significant scholarly attention in recent years, offering transformative possibilities for enhancing learning and teaching methodologies. In mathematics education, AI facilitates innovative pedagogical approaches that enable personalized learning experiences tailored to the diverse cognitive

profiles and needs of students, as demonstrated by empirical research on adaptive learning systems, learner-modeling algorithms, and AI-driven differentiation (e.g., Chen et al., 2020; Hwang et al., 2020). As educational demands evolve within the context of 21st-century skills, it is increasingly critical to equip learners with competencies necessary for addressing complex problem-solving scenarios and multi dimension (Hattie, 2009), wherein AI can function as a pivotal instructional tool. AI encompasses a broad spectrum of technological applications—ranging from intelligent tutoring systems to interactive chatbots—capable of mimicking cognitive functions essential for supporting and facilitating the learning process (Russell & Norvig, 2016).

Despite the rapid advancement and integration of AI technologies within general educational contexts, there remains a paucity of empirical research investigating their specific impact on metacognitive interactions in mathematics learning, particularly concerning advanced calculus topics such as the method of integration. Several scholars have noted a persistent paucity in AI integration within mathematics education, reflected in the tendency for AI-based interventions to remain tool- or outcome-centred rather than process-oriented (Opesemowo & Adewuyi, 2024), the insufficient measurement and operationalization of metacognitive interactions in AI-supported learning environments (Thi-Nga, 2024), and the continued presence of low-explainability feedback mechanisms that limit students' opportunities for reflection and self-regulation (Hwang et al., 2020). Mathematics instruction that predominantly employs teacher-led demonstrations of problem-solving procedures followed by individual practice remains commonplace; however, such pedagogical approaches frequently fail to accommodate the substantial variability in students' metacognitive engagement. Consequently, many learners are left insufficiently prepared to exercise effective self-regulation or to critically reflect upon the strategies they employ during mathematical problem solving. While existing literature emphasizes AI's potential to personalize learning environments, the intersection between AI-facilitated instruction and the development of students' metacognitive awareness and self-regulatory skills in higher-level mathematics remains underexplored (Luckin et al., 2016). This research seeks to address this gap by examining how AI-driven platforms influence students' engagement with metacognitive strategies in calculus, focusing on integration methods.

The primary objective of this study is to investigate the integration of AI technologies in fostering metacognitive interaction among students within mathematics education. Specifically, the research aims to elucidate how adaptive learning systems and interactive AI-based chat prompts can promote self-reflection, enhance personalized learning trajectories, and improve students' problem-solving capabilities. Through a qualitative exploration of students' lived experiences with AI tools, this study seeks to provide a nuanced understanding of how these technologies contribute to the development of metacognitive awareness and strategic thinking in mathematics learning contexts.

Guided by these objectives, the study addresses the following research questions: How do AI-driven platforms impact students' metacognitive awareness in mathematics education? The question concerns the mechanisms through which interactive chat-based prompts function as catalysts for learners' reflective thought and the enhancement of their problem-solving capacities, as well as how metacognitive processes are progressively constructed through iterative experiences of reflective engagement and cognitively demanding problem-solving activity. How do students perceive their learning experiences when utilizing AI technologies in mathematics? The hypotheses underpinning this research posit that: (1) the integration of AI technologies will positively influence students' metacognitive awareness and self-regulation in mathematics, and (2) students engaging with interactive AI tools will demonstrate enhanced reflective thinking and improved problem-solving skills compared to those exposed to traditional teaching methods.

LITERATURE REVIEW

Metacognition, defined as the awareness and regulation of one's cognitive processes, plays a pivotal role in effective learning and problem-solving, particularly within the discipline of mathematics (Flavell, 1979). Engaging with abstract mathematical concepts and multifaceted problem-solving tasks necessitates a high degree of metacognitive competence. Research consistently underscores the influence of metacognitive capabilities—including self-regulation, self-monitoring, and self-reflection—on academic performance across various domains, including mathematics (Schraw, 2001). For instance, students who actively engage in metacognitive practices, such as evaluating the efficacy of their problem-solving strategies or assessing their comprehension of mathematical concepts, tend to exhibit superior problem-solving effectiveness (Zimmerman, 2002). Instructional approaches that deliberately cultivate these skills empower learners to independently monitor their cognitive processes, adapt their problem-solving techniques, and ultimately achieve higher levels of academic success in mathematics (Brown, 1987).

This research holds considerable implications for the future trajectory of mathematics education, particularly in relation to the effective integration of AI technologies. The findings are anticipated to offer valuable insights into AI's role in enhancing student engagement, fostering self-regulation, and cultivating metacognitive skills. By foregrounding learners' experiences, the study aims to identify best practices for utilizing AI as a means of promoting educational equity, ensuring that all students—regardless of individual differences—have access to innovative and effective learning resources. Notably, a conceptual parallel can be drawn between the integration of AI in education and advanced integration techniques in higher calculus, such as those applied in calculating arc lengths, volumes, surface areas of revolution, and centroids. These mathematical methods involve systematically decomposing complex

integrals into more manageable components, a process analogous to breaking down intricate pedagogical challenges when incorporating AI.

In this way, the strategic application of AI technologies enables educators to optimize the learning experience incrementally, scaffolding cognitive development and promoting autonomous learning. Ultimately, this research contributes to a broader understanding of how AI can reshape educational methodologies, equipping students with essential cognitive and metacognitive skills to navigate the demands of an increasingly digital and complex world, while enhancing overall academic performance in mathematics.

RESEARCH METHODOLOGY

Research Design

This study adopts a qualitative case study methodology to explore the implementation of Artificial Intelligence (AI), with a particular focus on ChatGPT, in fostering metacognitive interaction within the context of the method of integration in mathematics. The case study design is well-suited for an in-depth investigation of intricate educational phenomena situated within authentic learning environments (Yin, 2018). This approach facilitates a comprehensive analysis of how AI-driven interventions influence students' metacognitive awareness, as well as their engagement with Personal Learning and Adaptive Learning strategies, thereby offering nuanced insights into the role of AI in enhancing mathematics learning experiences.

Metacognition Measurement

The measurement of metacognition in this study is systematically conducted through the application of the Metacognitive Awareness Inventory (MAI) developed by Schraw and Dennison (1994), a robust and extensively validated instrument. The MAI is designed to evaluate metacognitive awareness across two core dimensions: knowledge of cognition and regulation of cognition. The knowledge of cognition component is subdivided into declarative knowledge—pertaining to learners' explicit understanding of their cognitive abilities—procedural knowledge, which refers to their knowledge of strategy implementation, and conditional knowledge, which involves recognizing the appropriate contexts and timing for applying specific strategies. Concurrently, regulation of cognition encompasses essential self-regulatory processes, namely planning, monitoring, and evaluating, which collectively govern how learners control and adapt their cognitive strategies throughout the learning process (Heffernan and Heffernan, 2014).

To ensure the instrument's relevance and applicability within a domain-specific context, the present study employs the MAI in conjunction with mathematical problem-solving tasks, particularly focusing on the method of integration in calculus. By embedding the assessment within these integration problems, the study captures learners' real-time deployment of metacognitive strategies, offering insights into how they plan solution approaches, monitor

procedural accuracy, evaluate results, and flexibly apply declarative, procedural, and conditional knowledge. This integrative approach not only aligns the measurement tool with the cognitive demands of advanced mathematical tasks but also provides a nuanced understanding of how metacognitive awareness influences learners' ability to navigate complex problem-solving scenarios.

Participants

The participants in this study comprised eight Grade 12 students from a secondary school that implements AI-based learning tools within the Cambridge International Examination Curriculum, specifically those enrolled in Further Mathematics A Level. Participants were selected through purposive sampling (Creswell & Poth, 2018) to ensure their proficiency in calculus integration methods and their demonstrated metacognitive engagement. Throughout the study, all students consistently utilized AI chatbots to support the processes of planning, monitoring, and evaluation during instructional activities. Their sustained engagement offers valuable insights into how AI technologies influence pedagogical practices and promote learner autonomy, particularly concerning their interactions with advanced mathematical problem-solving and the application of metacognitive strategies.

Data Collection Methods

To ensure a comprehensive and nuanced understanding of how artificial intelligence (AI) facilitates metacognitive interaction in mathematics learning, this study adopted a multi-method qualitative research paradigm. Methodological triangulation was strategically implemented to fortify the credibility, transferability, and dependability of the findings, in alignment with the rigorous standards posited by Denzin and Lincoln (2018). Three principal data elicitation techniques were systematically orchestrated: semi-structured interviews, non-participant classroom observations, and documentary analysis.

The semi-structured interviews afforded an in-depth excavation of students' cognitive and metacognitive processes, yielding rich, phenomenologically descriptive narratives that illuminated their experiential engagement with AI-based learning tools. This approach not only surfaced students' perceptions of AI integration but also uncovered the latent cognitive mechanisms underpinning their interaction patterns.

Concurrently, non-participant classroom observations were meticulously conducted to capture real-time interaction dynamics, behavioral tendencies, and the operationalization of AI technologies within the instructional milieu. To ensure observational consistency and mitigate potential researcher bias, the observations were independently conducted by two trained observers, thereby enhancing inter-rater reliability and reinforcing the robustness of the data collection process. These observational data offered indispensable contextual insights, depicting

how students' engagement trajectories and learning behaviors evolved adaptively in response to AI-mediated pedagogical interventions.

Moreover, documentary analysis concentrated on students' completed mathematical tasks, specifically analyzing their problem-solving strategies. Each participant was systematically assigned five calculus problems pertaining to integration techniques, administered over five consecutive instructional sessions. Students solved one problem per session (50 minutes), utilizing AI-driven chatbot assistance, and subsequently composed reflective journals post-task. This iterative process yielded empirical evidence on their deployment of metacognitive strategies—encompassing planning, monitoring, and evaluation—and elucidated how AI tools scaffold reflective cognition.

Collectively, the integration of these qualitative elicitation methods ensured methodological rigor and presented a holistic, empirically substantiated portrayal of AI's transformative efficacy in fostering autonomous, reflective learning and augmenting higher-order cognitive competencies within the domain of mathematics education.

Semi-Structured Interviews

Interviews were conducted with eight Grade 12 students to explore their experiences, perceptions, and challenges regarding AI-enhanced metacognitive learning. The semi-structured format allowed for a flexible yet focused exploration of key issues while enabling participants to express their thoughts freely. The questions were designed to elicit insights into how AI influenced their learning processes, including their ability to plan, monitor, and regulate their problem-solving strategies. Sample interview questions included: How has AI influenced your ability to plan and monitor your learning in mathematics? In what ways has AI helped you reflect on and adjust your problem-solving strategies? What challenges have you encountered while using AI in mathematics learning?

These interviews provided rich, qualitative data that revealed the nuanced ways in which AI-supported learning technologies interact with students' metacognitive abilities. The teacher's responses further contextualized the findings, offering insights into pedagogical adjustments and the effectiveness of AI integration in the classroom.

Individual Observations

In addition to interviews, individual observations were systematically conducted to examine the interactions between students and AI tools during mathematics problem-solving tasks. Each observation session was structured, with students first working independently on mathematical problems for 20 minutes, followed by a 20-minute period where they consulted ChatGPT to review and verify their solutions. Subsequently, students were guided to reorganize their approaches and provide written reflections on their learning process. Two teacher

observers closely monitored each student throughout this sequence, focusing on individual engagement patterns, cognitive processes, and problem-solving behaviors as they navigated through each phase. This observational approach allowed for the real-time identification of metacognitive behaviors, adaptive learning strategies, and the nuances of student-teacher dynamics within an AI-supported instructional setting. The presence of both observers ensured a richer, triangulated perspective, capturing subtle variations in students' learning autonomy, strategy application, and responsiveness to instructional cues.

To complement these observations, detailed field notes were meticulously recorded to document critical instances of cognitive regulation, reflective evaluation, and problem-solving approaches. Additionally, video recordings were utilized to capture the intricacies of student interactions, enabling a comprehensive post-session analysis of self-regulation efforts and behavioral patterns. This multimodal data collection provided a robust foundation for identifying how AI tools facilitated adaptive feedback and supported students' metacognitive development. The integration of structured observation sessions, live field notes, and video analysis aligns with established qualitative methodologies, ensuring the reliability and depth of the findings (Merriam & Tisdell, 2016).

Document Analysis

To ensure methodological robustness and data validity, a triangulated approach was adopted by incorporating rubric-based assessments, semi-structured interviews, direct classroom observations, and document analysis. The use of standardized rubrics enabled a systematic evaluation of students' calculus problem-solving performance, specifically measuring key indicators such as procedural fluency, strategic application, and conceptual comprehension (Brookhart, 2018). This rubric-guided assessment provided quantifiable data reflecting the quality and depth of students' problem-solving processes, including the collection of their reflections and comments. In parallel, semi-structured interviews were conducted to capture students' reflective insights regarding their engagement with AI-based learning tools and problem-solving tasks. Direct observations during classroom sessions further enriched the dataset, offering contextual understanding of students' behaviors, collaborative interactions, and cognitive engagement during mathematics instruction (Creswell & Poth, 2018).

In addition to qualitative insights, document analysis was employed to examine learning analytics reports generated by AI-powered platforms, with particular focus on calculus problem-solving activities. These reports served as objective artifacts, detailing students' interaction histories, engagement patterns, and the frequency and efficiency of problem-solving attempts (Saldaña, 2021). Collectively, the integration of rubric evaluations, interview transcripts, observational field notes, and analytic reports allowed for a comprehensive, multi-dimensional analysis of student learning. This triangulation strategy ensured that the evaluation of students'

metacognitive and problem-solving development was both evidence-based and contextually grounded. By synthesizing these diverse data sources, the study presents a nuanced understanding of how AI tools mediate metacognitive interactions and foster higher-order thinking skills within mathematics education. Heffernan (2014). The following are the problems used in the method of integration.

Problem of Calculus Method of Integration

(Further mathematic Cambridge International Examination Curriculum)

Day 1 (50 menit)

1. The Polar equation of a curve C is $r = a(1 + \cos\theta)$ for $0 \leq \theta \leq 2\pi$, where a is a positive constant
 - (i) Sketch C
 - (ii) Show that the cartesian equation of C is $x^2 + y^2 = a(x + \sqrt{x^2 + y^2})$
 - (iii) Find area of the sector of C between $\theta = 0$ and $\theta = \frac{1}{3}\pi$
 - (iv) Find the arc length of C between the point where $\theta = 0$ and the point where $\theta = \frac{1}{3}\pi$
 Provide your comparison with the AI chatbot, reflect on the process, and revise your approach accordingly. What insights did you gain from this experience?

Day 2 (50 menit)

2. The curve C has equation $y = e^{-2x}$. Find, giving your answer correct to 3 significant figures
 - (i) The mean value of $\frac{dy}{dx}$ over the interval $0 \leq x \leq 2$
 - (ii) The coordinates of the centroid of the region bounded by C, $x = 0$, $x = 2$ and $y = 0$
 Provide your comparison with the AI chatbot, reflect on the process, and revise your approach accordingly. What insights did you gain from this experience?

Day 3 (50 menit)

3. The curve C has equation $y = \frac{1}{2}(e^x + e^{-x})$ For $0 \leq x \leq 4$
 - (i) The region R is bounded by C, the x-axis, the y-axis, and the line $x = 4$. Find, in terms of e, the coordinates of the centroid of the region R.
 - (ii) Show that:

$$\frac{ds}{dt} = \frac{1}{2}(e^x + e^{-x})$$

where s denotes the arc length of C, and find the surface area generated when C is rotated through 2π radians about the x-axis.

Provide your comparison with the AI chatbot, reflect on the process, and revise your approach accordingly. What insights did you gain from this experience?

Day 4 (50 menit)

4. The curve is defined parametrically by $x = t - \frac{1}{2}\sin 2t$ $y = \sin^2 t$
The arc of the curve joining the point where $t = 0$ to the point where $t = \pi$ is rotated through one complete revolution about the x axis. The area of the surface generated is denoted by S

(i) Show that $S = a\pi \int_0^\pi \sin^3 t \, dt$

Where the constant a is to be found.

(ii) Using the result $\sin 3t = 3\sin t - 4\sin^3 t$

Provide your comparison with the AI chatbot, reflect on the process, and revise your approach accordingly. What insights did you gain from this experience?

Day 5 (50 menit)

5. Starting from the definition of $\coth x$ and $\operatorname{cosech} x$ line.

(i) In terms of exponentials, prove that

$$\cot h^2 x - \operatorname{cosech}^2 x = 1$$

The curve C has equation $\frac{dy}{dx} = \ln \cot h\left(\frac{1}{2}x\right)$ for $x > 0$

(ii) show that $\frac{dy}{dx} = -\operatorname{cosech} x$

(iii) It is given that the arc length of C from $x = 0$ to $x = 2a$ is $\ln 4$, where a is a positive constant. Show that $\cosh a = 2$, in logarithmic form, find the exact value of a

Provide your comparison with the AI chatbot, reflect on the process, and revise your approach accordingly. What insights did you gain from this experience?

Data Analysis

The data analysis process encompassed a multi-method approach, involving the systematic evaluation of problem-solving outcomes, classroom observations, and in-depth interviews. In the analysis of problem-solving performance, a structured rubric was employed to assess the quality of students' solutions, focusing on critical indicators such as procedural accuracy, strategy application, and conceptual clarity (Brookhart, 2018). Additionally, qualitative annotations and comments embedded within the students' responses were meticulously examined to capture their reasoning patterns and metacognitive reflections. Observational data were collected by closely scrutinizing students' approaches and strategies during task completion, allowing the researchers to document real-time cognitive behaviors, collaboration dynamics, and adaptive problem-solving techniques (Creswell & Poth, 2018).

For the interview data, thematic analysis was applied, following Braun and Clarke's (2021) established framework, to systematically interpret the participants' perspectives. An inductive coding methodology guided the analytical process, enabling salient patterns and themes to naturally emerge from the data corpus. The thematic analysis progressed through four critical stages: (1) data familiarization, involving iterative reviews of transcripts, observation logs, and related documents to gain comprehensive insights; (2) initial coding, wherein recurrent patterns related to AI-mediated metacognitive interactions were identified; (3) theme development, grouping codes into overarching categories such as AI-assisted self-regulation, adaptive feedback mechanisms, and cognitive reflection strategies; and (4) interpretation and synthesis, wherein emergent themes were analyzed against extant theoretical frameworks on AI in education and metacognitive learning. To bolster the trustworthiness of the findings, methodological

triangulation was implemented (Denzin, 2017), integrating data from interviews, observations, and document analyses. This triangulated strategy ensured analytical rigor and enhanced the credibility of conclusions drawn regarding AI's role in fostering metacognitive engagement in mathematics education.

DISCUSSION

The thematic analysis of the interview transcripts, corroborated by observational and documentary data, yielded salient insights into the integral role of metacognition within self-regulated learning frameworks. Our findings underscore that metacognition constitutes a pivotal construct in fostering autonomous learning, encapsulating an individual's capacity to consciously monitor, regulate, and evaluate their cognitive processes. In the milieu of mathematics education, AI-augmented learning environments demonstrably function as dynamic scaffolds, systematically enhancing students' metacognitive engagement. This facilitation is manifested through the amplification of learners' abilities to introspectively reflect upon their reasoning, strategically adjust their learning trajectories, and iteratively refine their problem-solving competencies.

Three core dimensions of metacognition—namely, metacognitive awareness, cognitive regulation, and reflective evaluation—emerged as instrumental in cultivating independent and cognitively agile learners. These dimensions collectively underpin the development of cognitive flexibility, equipping students with the requisite analytical acuity to adeptly navigate complex and abstract mathematical constructs.

The integration of AI-driven educational technologies exerts a transformative influence on mathematics instruction by catalyzing personalized, student-centered learning pathways. AI-facilitated autonomy empowers learners to self-direct their educational experiences, granting them agency over the selection of instructional materials, problem-solving methodologies, and pacing strategies congruent with their cognitive profiles. This personalization is operationalized through adaptive feedback loops, intelligent tutoring systems, and real-time learning analytics, ensuring that students receive granular, data-driven support calibrated to their evolving proficiency levels.

Moreover, AI-enabled differentiation within the mathematics curriculum enables precise content customization, informed by continuous analysis of learner behavior and academic readiness. This pedagogical flexibility ensures that instructional delivery is tailored to optimize student engagement, knowledge retention, and conceptual mastery. The deployment of these adaptive learning mechanisms engenders enriched metacognitive development, as real-time scaffolding and individualized feedback create conducive conditions for deeper comprehension, procedural fluency, and reflective learning practices.

The findings further reveal that AI-powered adaptive learning environments bolster students' responsiveness to cognitive challenges by fostering iterative feedback cycles and promoting technological personalization. Such environments are characterized by their capacity to dynamically adjust instructional complexity, thereby accommodating learners' diverse problem-solving proficiencies. Through predictive analytics, AI systems identify potential learning gaps and modulate content delivery to fortify both foundational and advanced mathematical competencies.

In consonance with the broader literature, these results affirm that AI integration substantively enhances metacognitive interaction, enabling students to accurately identify cognitive strengths and limitations while strategically deploying effective problem-solving strategies. Consequently, AI-mediated learning paradigms not only contribute to elevating students' mathematical performance but also advance the frontiers of innovative, technology-enhanced educational practice.

This thematic framework provides a comprehensive understanding of how AI facilitates metacognitive interaction by fostering self-regulation, personalized learning pathways, and adaptive instructional support. Three respondents testified that they learned significantly from how AI guided them to solve problems in a more structured manner. Four respondents reported that they acquired new problem-solving strategies through their engagement with AI, while one respondent noted that observing AI-generated solutions helped them cultivate creativity in approaching the tasks. Future research should further investigate the long-term effects of AI-based interventions on students' metacognitive development, taking into account both the cognitive and affective dimensions of learning engagement.

The thematic hierarchical model organizes learning components into structured categories, enhancing clarity in educational research and curriculum design. It helps educators analyze metacognition, personal learning, and adaptive learning systematically. This model supports personalized learning, effective strategy development, and technology integration, improving teaching methodologies and student learning outcomes efficiently.

Table 1. Thematic Finding

No	Theme	Dimension	Description from observation
1.	Metacognition	Metacognitive Awareness	Students show an awareness of how they think and learn. They recognize their strengths and areas for improvement, and actively develop strategies to make their learning more effective.
		Cognitive Regulation	Students are able to manage their learning by planning ahead, keeping track of their progress, solving problems along the way, and evaluating their performance to stay on track and continuously improve.
		Reflective Evaluation	Students engage in regular reflection on the learning strategies they have employed, thoughtfully evaluating what was effective and what was not. Drawing on these insights, they make informed adjustments to refine their approach for the next learning strategy.
2.	Personal Learning	Learning Autonomy	Students take ownership of their learning process. They choose their own materials, decide on the best strategies, solve problems independently, and set their own pace to match their preferences.
		Learning Preferences and Styles	Each student demonstrates unique cognitive tendencies and learning styles, which support more meaningful and personalized learning experiences.
		Curriculum Differentiation	Flexibility is provided within the curriculum, allowing students to choose learning paths that best suit their individual needs and interests.
3.	Adaptive Learning	Response to Change	Students show adaptability when faced with changes in the learning environment—whether it's new technology, different learning strategies, or the creative structuring and problem-solving involved in integrating methods in calculus.
		Continuous Feedback	There is an ongoing feedback process where students receive regular input on their progress, helping them refine their learning methods and materials in real time.
		Technology in Adaptive Learning	Technology, including AI and digital platforms, is used to personalize learning by analyzing each student's performance and tailoring content to meet their specific needs.

CONCLUSION

The findings and results reveal conclusions that encompass not only the specific implementation within integral calculus, particularly the method of integration, but also offer broader implications for mathematics education in the expansion of subsequent research.

Our investigation confirms that AI-driven adaptive learning systems significantly enhance metacognitive interaction in mathematics education, emphasizing the pivotal role of self-regulated learning in academic success. The study highlights how interactive chat prompts and real-time feedback empower students to reflect on their problem-solving approaches, monitor their cognitive processes, and refine their strategic thinking—ultimately deepening their grasp of complex mathematical concepts.

Furthermore, the findings indicate that AI integration not only facilitates the identification of individual cognitive strengths and weaknesses but also fosters critical thinking and robust problem-solving abilities. By offering personalized learning pathways, these systems adapt dynamically to students' needs, promoting engagement, autonomy, and mastery of mathematical reasoning.

Given these insights, it is strongly recommended that educational institutions integrate AI-based platforms to customize instruction, optimize feedback mechanisms, and enhance adaptive learning experiences. This entails not only the deployment of advanced AI tools but also comprehensive educator training to ensure effective implementation. Additionally, continuous performance assessment protocols should be established to measure and refine AI-driven interventions. Ultimately, AI's integration into mathematics education does more than support metacognitive growth—it nurtures independent, adaptable learners capable of navigating the evolving challenges of modern mathematical inquiry with confidence and precision.

Implementation

To effectively implement AI-driven adaptive learning in mathematics education, institutions should integrate AI-powered platforms that offer personalized learning, real-time feedback, and adaptive problem-solving pathways. Educators must receive targeted training to leverage AI insights, ensuring seamless integration with existing curricula. AI tools should diagnose individual student needs, enabling differentiated instruction and self-regulated learning while fostering deeper conceptual understanding.

Continuous monitoring and assessment are essential to measure AI's impact on learning outcomes and refine instructional strategies. Ethical considerations, including data privacy and responsible AI use, must be prioritized to maintain a balanced, student-centered approach. By leveraging AI effectively, institutions can cultivate critical thinking, metacognitive skills, and independent problem-solving abilities, preparing students for the challenges of modern mathematics.

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